

| Question | | | Answer | Marks | AO | Guidance |
|----------|--|--|--|------------|-------------|---|
| 13 | | | $2y \frac{dy}{dx}$ | B1 | 1.1 | chain rule |
| | | | $y + x \frac{dy}{dx}$ | B1 | 3.1a | product rule |
| | | | (their previous terms) $+ 2x - 1 = 0$ | B1 | 1.1 | may award if “= 0” seen later, but not if RHS is $\frac{dy}{dx}$ |
| | | | their $y + 2x - 1 = 0$ | M1 | 2.1 | substitution of $\frac{dy}{dx} = 0$; may follow (incorrect) rearrangement; dependent on award of at least one B mark NB $\frac{dy}{dx} = \frac{1-2x-y}{2y+x}$ |
| | | | $(1 - 2x)^2 + x(1 - 2x) + x^2 - x = 1$ | M1 | 3.1a | elimination of x or y using expression or value obtained from use of $\frac{dy}{dx} = 0$; dependent on award of at least one B mark |
| | | | or $y^2 + \frac{(1-y)y}{2} + \frac{(1-y)^2}{4} - \frac{1-y}{2} = 1$ | | | |
| | | | $3x^2 - 4x [= 0]$ or $3y^2 + 2y - 5 [= 0]$ | A1 | 1.1 | |
| | | | $x = 0, x = \frac{4}{3}$ | M1 | 1.1 | values of x or y found from their quadratic |
| | | | $y = 1, y = -\frac{5}{3}$ | M1 | 1.1 | values of y or x found from substitution of both x or both y values; must see substitution unless values correct NB may see extra points $y = -1$ or $\frac{1}{3}$ from substitution into original equation |
| | | | $(0,1)$ and $\left(\frac{4}{3}, -\frac{5}{3}\right)$ or $x = 0, y = 1$ and $x = \frac{4}{3}, y = -\frac{5}{3}$ | A1 | 3.2a | A0 if extra points in final answer; dependent on fully correct working throughout; if M0M0 allow SCB1 for 1 correct pair of coordinates and no others |
| | | | | [9] | | |

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|----------|--|--|--|---|----|--|
| | | | <i>Alternatively</i> $2x \frac{dx}{dy} - \frac{dx}{dy}$ $x + y \frac{dx}{dy}$ (their previous terms) $+2y = 0$ their $1 - 2x - y = 0$ $(1 - 2x)^2 + x(1 - 2x) + x^2 - x = 1$ or $y^2 + \frac{(1-y)y}{2} + \frac{(1-y)^2}{4} - \frac{1-y}{2} = 1$ $3x^2 - 4x [= 0] \text{ or } 3y^2 + 2y - 5 [= 0]$ $x = 0, x = \frac{4}{3}$ $y = 1, y = -\frac{5}{3}$ $(0,1) \text{ and } \left(\frac{4}{3}, -\frac{5}{3}\right) \text{ or}$ $x = 0, y = 1 \text{ and } x = \frac{4}{3}, y = -\frac{5}{3}$ | B1 B1 B1 M1 M1 A1 M1 M1 A1 | | chain rule product rule may award if “= 0” seen later, but not if RHS is $\frac{dy}{dx}$ from setting denominator of $\frac{dx}{dy} = \frac{2y+x}{1-2x-y}$ equal to 0 or rearranging to find $\frac{dy}{dx} = \frac{1-2x-y}{2y+x}$ and setting equal to 0; dependent on award of at least one B mark elimination of x or y using expression or value obtained from use of $\frac{dy}{dx} = 0$; dependent on award of at least one B mark values of x or y found from their quadratic values of y or x found from substitution of both x or both y values; must see substitution unless values correct NB may see extra points $y = -1$ or $\frac{1}{3}$ from substitution into original equation A0 if extra points in final answer; dependent on fully correct working throughout if M0M0 allow SCB1 for 1 correct pair of coordinates and no others |
| | | | | 9 | | |