

9 The gradient of a curve is given by  $\frac{dy}{dx} = e^x - 4e^{-x}$ .

(a) Show that the  $x$ -coordinate of any point on the curve at which the gradient is 3 satisfies the equation  $(e^x)^2 - 3e^x - 4 = 0$ . [2]

(b) Hence show that there is only one point on the curve at which the gradient is 3, stating the exact value of its  $x$ -coordinate. [3]

(c) The curve passes through the point  $(0, 0)$ .

Show that when  $x = 1$  the curve is below the  $x$ -axis. [5]