

6	(a)	DR		M1	1.1	$4xy = 2(x^2 + 4y^2) - 9x$	
		$4y + 4x \frac{dy}{dx} = 4x + 16y \frac{dy}{dx} - 9$ $4x \frac{dy}{dx} - 16y \frac{dy}{dx} = 4x - 4y - 9 \Rightarrow \frac{dy}{dx} = \frac{4x - 4y - 9}{4x - 16y}$		A1	1.1	For correct differentiation of either LHS or RHS, even if not in an equation	
				A1	2.1	AG (at least one line of working from correct differentiation to given answer)	
				[3]			
6	(b)	<p>DR</p> <p>(At P) $4x - 16y = 0$</p> <p>$x = 4y \Rightarrow 16y^2 = 2(16y^2 + 4y^2) - 36y$</p> <p>$24y^2 - 36y = 0$</p> <p>$y(2y - 3) = 0 \Rightarrow y = \frac{3}{2}$</p> <p>$P\left(6, \frac{3}{2}\right)$</p> <p>(At Q) $4x - 4y - 9 = 0$</p> <p>$\Rightarrow 4x\left(x - \frac{9}{4}\right) = 2x^2 + 8\left(x - \frac{9}{4}\right)^2 - 9x$</p> <p>$4x^2 - 24x + 27 = 0$</p> <p>$Q\left(\frac{3}{2}, -\frac{3}{4}\right)$ only</p> <p>$PQ^2 = \left(6 - \frac{3}{2}\right)^2 + \left(\frac{3}{2} - \left(-\frac{3}{4}\right)\right)^2$</p> <p>$PQ = \frac{9}{4}\sqrt{5}$</p>		M1*	3.1a		
				M1dep*	2.1	Forms two-term quadratic equation in y or x (if correct $x^2 - 6x = 0$)	
				A1	1.1		$y \neq 0$ not required
				M1*	3.1a		
				M1dep*	2.1	Forms three-term quadratic equation in y or x (if correct $16y^2 - 24y - 27 = 0$)	
				A1	3.2a		
				M1	1.1	Correct implies distance formula for their P and Q	
				A1	2.2a		
				[8]			