

11 The gradient function of a curve is given by $\frac{dy}{dx} = \frac{3x^2 \ln x}{e^{3y}}$.

The curve passes through the point $(e, 1)$.

(a) Find the equation of this curve, giving your answer in the form $e^{3y} = f(x)$. **[6]**

(b) Show that, when $x = e^2$, the y -coordinate of this curve can be written as $y = a + \frac{1}{3} \ln(b e^3 + c)$, where a , b and c are constants to be determined. **[3]**