(a) Use the substitution $u^2 = x^2 + 3$ to show that $\int \frac{4x^3}{\sqrt{x^2 + 3}} dx = \frac{4}{3}(x^2 - 6)\sqrt{x^2 + 3} + c$.

(b) In this question you must show detailed reasoning.

[5]

The graph shows part of the curve $y = \frac{4x^3}{\sqrt{x^2 + 2}}$. Find the exact area enclosed by the curve $y = \frac{4x^3}{\sqrt{x^2 + 3}}$, the normal to this curve at the point (1, 2) and the x-axis.

POST-EXAM CORRECTION

Wednesday 6 October 2021 - Afternoon

A Level Mathematics A

H240/01 Pure Mathematics

If you wish to use the published question paper as practice material, please make the following correction:

In the first line below the graph cross out $y = \frac{4x^3}{\sqrt{x^2 + 2}}$ and replace it with $y = \frac{4x^3}{\sqrt{x^2 + 3}}$.

Turn to page 7 of the question paper and look at question 11(b).

The question should now read:

The graph shows part of the curve
$$y = \frac{4x^3}{\sqrt{x^2 + 3}}$$
.