

The diagram shows the curve C with equation $y = 4x^2 - 10x + 7$ and two straight lines, l_1 and l_2 . The line l_1 is the normal to C at the point $\left(\frac{1}{2},3\right)$. The line l_2 is the normal to C at the minimum point of C.

(a) Determine the equation of l_1 , giving your answer in the form ax + by + c = 0, where a, b and c are integers to be determined. [4]

[3]

The shaded region shown in the diagram is bounded by C, l_1 and l_2 .

(b) Determine the inequalities that define the shaded region, including its boundaries.