

Question	Scheme	Marks	AOs
<b>10(a)</b>	$8(4) - 4^{\frac{5}{2}} = 32 - 32 = 0$	B1	1.1b
		(1)	
<b>(b)</b>	$8 - \frac{5}{2}x^{\frac{3}{2}}$	B1	1.1b
	$x = 4 \Rightarrow \left\{ \frac{dy}{dx} = \right\} 8 - \frac{5}{2} \times 8 = -12$ $\Rightarrow y\{-0\} = "-12"(x-4)$	M1	1.1b
	$12x + y = 48$ *	A1*	1.1b
		(3)	
<b>(c)</b>	Attempts to find one of the coordinates of the point of intersection $y = 8x, 12x + y = 48 \Rightarrow y = 19.2$ (or $x = 2.4$ )	M1	1.1b
	Triangle area is $\frac{1}{2} \times 4 \times "19.2" (= 38.4 \text{ or } \frac{192}{5})$ or $\int_0^{2.4} 8x \, dx + \int_{2.4}^4 "(48 - 12x)" \, dx$	dM1	3.1a
	$\int \left( 8x - x^{\frac{5}{2}} \right) dx = 4x^2 - \frac{2}{7}x^{\frac{7}{2}}$	B1	1.1b
	$A = 38.4 - \left[ "4x^2 - \frac{2}{7}x^{\frac{7}{2}}" \right]_0^4 = 38.4 - 64 + \frac{256}{7}$	ddM1	3.1a
	$= \frac{384}{35}$	A1	1.1b
		(5)	

(9 marks)

### Notes

(a)

**B1:** Substitutes  $x = 4$  into the equation of the curve and verifies that  $y = 0$ . Accept " $8(4) - 4^{\frac{5}{2}} = 0$ "  
Alternatively, sets  $8x - x^{\frac{5}{2}} = 0$  and solves with correct processing to achieve  $x = 4$ .  
As a minimum accept e.g.  $8x - x^{\frac{5}{2}} = 0 \Rightarrow x^{\frac{3}{2}} = 8 \Rightarrow \{x = \} 4$  which may follow factorisation.

(b)

**B1:** Correct differentiation. The  $\frac{dy}{dx} =$  need not be present.

**M1:** Correct method for finding the equation of the tangent at  $A(4, 0)$ .

Requires substitution of  $x = 4$  into their  $\frac{dy}{dx}$  and an attempt at the equation of the line using this gradient. If using  $y - y_1 = m(x - x_1)$  then condone the omission of the  $- 0$ .

If  $y = mx + c$  is used they must proceed as far as  $c = \dots$

Accept  $\frac{dy}{dx} = -12$  or  $m = -12$  without explicit substitution of  $x = 4$  provided  $8 - \frac{5}{2}x^{\frac{3}{2}}$  is seen.

**A1\*:** Correct work leading to the given equation having scored B1M1.

Condone  $y + 12x = 48$  and apply isw once seen.

Do not condone  $12x + y - 48 = 0$  (unless a correct equation  $= 48$  is seen).

(c) **Note:** Condone poor notation such as missing  $dx$  or spurious  $\int$  symbols throughout.

**M1:** Attempts to find either the  $x$  or  $y$  coordinate of the intersection of line  $l_1$  and line  $l_2$   
You may need to check the diagram or limits to their integrals.

**dM1:** Correct method for the area of the triangle. e.g. Triangle area is  $\frac{1}{2} \times 4 \times "19.2" \left( = 38.4 \text{ or } \frac{192}{5} \right)$

If integration is attempted then condone slips in their rearrangement of  $12x + y = 48$  to  $y = 48 - 12x$  and note that their integrals do need not to be evaluated, so for example

$$\text{look for } \int_0^{"2.4"} 8x \, dx + \int_{"2.4"}^4 "(48 - 12x)" \, dx \quad \left\{ = \frac{576}{25} + \frac{384}{25} = 23.04 + 15.36 \right\}$$

**B1:** Correct integration of **curve** ignoring limits, i.e.  $4x^2 - \frac{2}{7}x^{\frac{7}{2}}$  but condone e.g.  $\frac{8x^{1+1}}{2} - \frac{x^{\frac{5}{2}+1}}{\frac{7}{2}}$

**ddM1:** Fully correct strategy including substitution which would lead to an **exact** area.

Does not need to reach a value. Dependent on both previous M marks.

$$\text{Implied by } 38.4 - \frac{192}{7} \text{ or a correct final answer } \frac{384}{35}$$

Note that the decimal approximation that might be seen is 10.97142857 and implies ddM0 unless there is evidence of substitution (which need not be evaluated).

**A1:** Correct exact value. Either  $\frac{384}{35}$  or  $10\frac{34}{35}$

### Alternative using lines – curve:

**M1:** Attempts to find either the  $x$  or  $y$  coordinate of the intersection of line  $l_1$  and line  $l_2$   
You may need to check the diagram or limits to their integrals.

**dM1:** Correct method for at least one part (0 to "2.4" or "2.4" to 4) of the area of  $R$  including limits.  
Condone slips in their rearrangement of  $12x + y = 48$  to  $y = 48 - 12x$  and note that their integrals do need not to be evaluated, so for example

$$\text{look for } \int_0^{"2.4"} 8x - \left( 8x - x^{\frac{5}{2}} \right) dx \text{ or } \int_{"2.4"}^4 "(48 - 12x) - \left( 8x - x^{\frac{5}{2}} \right) dx \text{ (or a sum of both)}$$

**B1:** Correct integration of **both** regions ignoring limits. May be completed as a sum or separately.

Condone e.g.  $\frac{x^{\frac{5}{2}+1}}{\frac{7}{2}}$  in place of  $\frac{2}{7}x^{\frac{7}{2}}$  Note that each integral may have been simplified.

$$\int_{\dots}^{\dots} x^{\frac{5}{2}} dx \text{ and } \{+\} \int_{\dots}^{\dots} 48 - 20x + x^{\frac{5}{2}} dx \rightarrow \left[ \frac{2}{7}x^{\frac{7}{2}} \right]_{\dots}^{\dots} \text{ and } \{+\} \left[ 48x - 10x^2 + \frac{2}{7}x^{\frac{7}{2}} \right]_{\dots}^{\dots}$$

**ddM1:** Fully correct strategy including substitution which would lead to an **exact** area.

Does not need to reach a value. Dependent on both previous M marks.

This approach requires:

- substitution of 0, their 2.4 and 4 in the correct places

- the  $\frac{2}{7}(2.4)^{\frac{7}{2}} - \frac{2}{7}(2.4)^{\frac{7}{2}}$  to be cancelled (may be implied by a correct final answer  $\frac{384}{35}$ )

Note that the decimal approximation that might be seen is 10.97142857 and implies ddM0

unless there is evidence that the  $\frac{2}{7}(2.4)^{\frac{7}{2}} - \frac{2}{7}(2.4)^{\frac{7}{2}}$  has been cancelled e.g. ~~6.118... - 6.118...~~

**A1:** Correct exact value. Either  $\frac{384}{35}$  or  $10\frac{34}{35}$