

Question	Scheme	Marks	AOs
12(a)	$\int x^2 e^{x^3} dx = \frac{1}{3} e^{x^3} (+c)$	M1 A1	1.1b 1.1b
	(2)		
(b)	$u = x^3 \Rightarrow \frac{du}{dx} = 3x^2 \Rightarrow \int x^8 e^{x^3} dx = \int \frac{x^8 e^u}{3x^2} du = \frac{1}{3} \int u^2 e^u du$	M1	3.1a
	$\frac{1}{3} \int u^2 e^u du = \frac{1}{3} u^2 e^u - \frac{2}{3} \int ue^u dx$	M1 A1	2.1 1.1b
	$= \frac{1}{3} u^2 e^u - \frac{2}{3} ue^u + \frac{2}{3} \int e^u du$	M1	1.1b
	$= \frac{1}{3} u^2 e^u - \frac{2}{3} ue^u + \frac{2}{3} e^u + c = \frac{1}{3} x^6 e^{x^3} - \frac{2}{3} x^3 e^{x^3} + \frac{2}{3} e^{x^3} + c$	A1	2.1
	$= \frac{1}{3} e^{x^3} (x^6 - 2x^3 + 2) + c$		
	(5)		
	Alternative:		
	$\int x^8 e^{x^3} dx = \int x^6 x^2 e^{x^3} dx$	M1	3.1a
	$\int x^6 x^2 e^{x^3} dx = \frac{1}{3} x^6 e^{x^3} - 2 \int x^5 e^{x^3} dx$	M1 A1	2.1 1.1b
	$\int x^6 x^2 e^{x^3} dx = \frac{1}{3} x^6 e^{x^3} - 2 \int x^3 x^2 e^{x^3} dx$	M1	1.1b
	$= \frac{1}{3} x^6 e^{x^3} - 2 \left[\frac{1}{3} x^3 e^{x^3} - \int x^2 e^{x^3} dx \right]$		
	$= \frac{1}{3} x^6 e^{x^3} - \frac{2}{3} x^3 e^{x^3} + \frac{2}{3} e^{x^3} + c = \frac{1}{3} e^{x^3} (x^6 - 2x^3 + 2) + c$	A1	2.1

(7 marks)

Notes

(a)

M1: For $\int x^2 e^{x^3} dx = k e^{x^3} (+c)$

A1: Correct integration (condone omission of $+ c$)

(b)

M1: Fully correct strategy for the substitution to reach an integral in terms of u only.

M1: Applies integration by parts in the correct direction on $u^2 e^u$

A1: Correct integral for the first application of parts

M1: Applies parts again on ue^u

A1: Completes the process and obtains the correct answer in the form required

Alt:

M1: Makes the key step of writing x^8 as $x^6 \times x^2$

M1: Applies integration by parts in the correct direction

A1: Correct integral for the first application of parts

M1: Applies integration by parts again, in the correct direction, after writing x^5 as $x^3 \times x^2$

A1: Completes the process and obtains the correct answer in the form required