Question	Scheme	Marks	AOs
3 (a)	(i) $x^2 + y^2 - 10x + 16y = 80 \Rightarrow (x-5)^2 + (y+8)^2 =$	M1	1.1b
	Centre $(5, -8)$	A1	1.1b
	(ii) Radius 13	A1	1.1b
		(3)	
(b)	Attempts $\sqrt{"5"^2 + "8"^2} + "13"$	M1	3.1a
	$13 + \sqrt{89}$ but ft on their centre and radius	A1ft	1.1b
		(2)	
			(5 marks)
Notes:			

(a)(i)

M1: Attempts to complete the square on **both** *x* and *y* terms.

Accept 
$$(x \pm 5)^2 + (y \pm 8)^2 = \dots$$
 or imply this mark for a centre of  $(\pm 5, \pm 8)$ 

Condone 
$$(x \pm 5)^2 \dots (y \pm 8)^2 = \dots$$
 where the first ... could be, or even –

A1: Correct centre (5, -8).

Accept without brackets. May be written x = 5, y = -8 (a)(ii)

A1: 13. The M mark must have been awarded, so it can be scored following a centre of  $(\pm 5, \pm 8)$ . Do not allow for  $\sqrt{169}$  or  $\pm 13$ 

M1: Attempts  $\sqrt{5^{*}+8^{*}} + 13^{*}$  for their centre (5,-8) and their radius 13.

Award when this is given as a decimal, e.g. 22.4 for correct centre and radius. Look for  $\sqrt{a^2 + b^2} + r$  where centre is  $(\pm a, \pm b)$  and radius is r

A1ft:  $13 + \sqrt{89}$  Follow through on their (5, -8) and their 13 leading to an exact answer. ISW for example if they write  $13 + \sqrt{89} = 22.4$ 



There are more complicated attempts which could involve finding *P* by solving  $y = "-\frac{8}{5}x"$  and

 $x^2 + y^2 - 10x + 16y = 80$  simultaneously and choosing the coordinate with the greatest modulus. The method is only scored when the distance of the largest coordinate from *O* is attempted. Such methods are unlikely to result in an exact value but can score 1 mark for the method. Condone slips

FYI. Solving 
$$y = -\frac{8}{5}x$$
 and  $x^2 + y^2 - 10x + 16y = 80 \Rightarrow 89x^2 - 890x - 2000 = 0 \Rightarrow P = (11.89, -19.02)$   
Hence  $OP = \sqrt{"11.89"^2 + "19.02"^2} (= 22.43)$  scores M1 A0 but  $OP = \sqrt{258 + 26\sqrt{89}}$  is M1 A1