

Figure 3

Figure 3 shows a sketch of the curve with equation $y = 2^{x^2} - x$

The finite region R, shown shaded in Figure 3, is bounded by the curve, the line with equation x = -0.5, the x-axis and the line with equation x = 1.5

(a) Use the trapezium rule with four strips of equal width to find an estimate for the area of R. Show your working and give your answer to two decimal places.

(4)

A copy of Figure 3, called Diagram 1, is drawn below.

(b) Explain, with the aid of Diagram 1, whether your answer in part (a) is an underestimate or overestimate of the true value for the area of R.

(1)

Using your answer to part (a) and showing your working,

(c) estimate the value of
$$\int_{-0.5}^{1.5} (2^{x^2+1} + 2x) dx$$
 (3)

