

Figure 7 shows a sketch of the curve with equation

$$y = 4xe^{-2x} \qquad x \geqslant 0$$

The line *l* is the normal to the curve at the point $P(1, 4e^{-2})$

The finite region R, shown shaded in Figure 7, is bounded by the curve, the line l, and the x-axis.

Find the exact value of the area of R.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(10)