

Figure 4 shows a bowl with a circular cross-section.

Initially the bowl is empty. Water begins to flow into the bowl.

At time t seconds after the water begins to flow into the bowl, the height of the water in the bowl is $h \, \text{cm}$.

The volume of water, $V \text{cm}^3$, in the bowl is modelled as

$$V = 4\pi h(h+6) \qquad 0 \leqslant h \leqslant 25$$

The water flows into the bowl at a constant rate of 80π cm³ s⁻¹

(a) Show that, according to the model, it takes 36 seconds to fill the bowl with water from empty to a height of 24 cm.

(b) Find, according to the model, the rate of change of the height of the water, in cm s⁻¹, when t = 8

(8)

(1)