

Question	Scheme	Marks	AOs
13 (a)	$\begin{aligned}\sum_{n=1}^{11} \ln(p^n) &= \ln p + \ln p^2 + \ln p^3 + \dots + \ln p^{11} \\ &= \ln p + 2\ln p + 3\ln p + \dots + 11\ln p \\ &= \frac{11}{2}(2\ln p + (11-1)\ln p) \quad \text{or} \quad \frac{1}{2}(11)(12)\ln p\end{aligned}$	M1	3.1a
	$= 66\ln p \quad \{k = 66\}$		A1
			(2)
(b)	$\begin{aligned}S &= \sum_{n=1}^{11} \ln(8p^n) = \ln 8p + \ln 8p^2 + \ln 8p^3 + \dots + \ln 8p^{11} \\ &= 11\ln 8 + 66\ln p\end{aligned}$	M1	1.1b
(c)	e.g.	A1*	2.1
	<ul style="list-style-type: none"> • $11\ln 8 + 66\ln p = 11\ln 2^3 + 66\ln p = 33\ln 2 + 66\ln p$ $= 33(\ln 2 + 2\ln p) = 33(\ln 2 + \ln p^2) = 33\ln(2p^2) *$ • $11\ln 8 + 66\ln p = 11\ln 2^3 + 66\ln p = 33\ln 2 + 66\ln p$ $= \ln(2^{33} p^{66}) = \ln((2p^2)^{33}) = 33\ln(2p^2) *$ 		
			(2)
	$S < 0 \Rightarrow 33\ln(2p^2) < 0 \Rightarrow \ln(2p^2) < 0$ so either $0 < 2p^2 < 1$ or $2p^2 < 1$ $\Rightarrow p^2 < \frac{1}{2}$ and $p > 0 \Rightarrow 0 < p < \frac{1}{\sqrt{2}}$ In set notation, e.g. $\left\{ p : 0 < p < \frac{1}{\sqrt{2}} \right\}$	M1	2.2a
		A1	2.5
			(2)
(6 marks)			

Question 13 Notes:**(a)****M1:**

Attempts to find $\sum_{n=1}^{11} \ln(p^n)$ by using a complete strategy of

- applying the power law of logarithms

followed by either

- applying the correct formula for the sum to n terms of an arithmetic series
- applying the correct formula $\frac{1}{2}n(n+1)\ln p$
- summing the individual terms to give $66\ln p$

A1:

$66\ln p$ from correct working

(b)**M1:**

Deduces S or $\sum_{n=1}^{11} \ln(8p^n) = 11\ln 8 + (\text{their answer to part (a)})$

A1*:

and produces a logical argument to correctly show that $S = 33\ln(2p^2)$ with no errors seen

(c)**M1:**

Applies $S < 0$ to give $\ln(2p^2) < 0$ and deduces {e.g. by considering the graph of $y = \ln x$ } that either

- $0 < 2p^2 < 1$
- $2p^2 < 1$

A1:

Correct answer using set notation. E.g.

- $\left\{ p : 0 < p < \frac{1}{\sqrt{2}} \right\}$
- $\left\{ p : 0 < p < \frac{\sqrt{2}}{2} \right\}$
- $\{p : p > 0\} \cap \left\{ p : p < \frac{1}{\sqrt{2}} \right\}$
- $\{p : p > 0\} \cap \left\{ p : p < \frac{\sqrt{2}}{2} \right\}$