

12.

In this question you should show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for $0 < \theta \leq 450^\circ$, the equation

$$5 \cos^2 \theta = 6 \sin \theta$$

giving your answers to one decimal place.

(5)

(ii) (a) A student's attempt to solve the question

“Solve, for $-90^\circ < x < 90^\circ$, the equation $3 \tan x - 5 \sin x = 0$ ”

is set out below.

$$\begin{aligned}
 3 \tan x - 5 \sin x &= 0 \\
 3 \frac{\sin x}{\cos x} - 5 \sin x &= 0 \\
 3 \sin x - 5 \sin x \cos x &= 0 \\
 3 - 5 \cos x &= 0 \\
 \cos x &= \frac{3}{5} \\
 x &= 53.1^\circ
 \end{aligned}$$

Identify two errors or omissions made by this student, giving a brief explanation of each.

(2)

The first four positive solutions, in order of size, of the equation

$$\cos(5\alpha + 40^\circ) = \frac{3}{5}$$

are $\alpha_1, \alpha_2, \alpha_3$ and α_4 (b) Find, to the nearest degree, the value of α_4

(2)