

Figure 4

Figure 4 shows a sketch of part of the curve C with equation

$$y = \frac{32}{x^2} + 3x - 8, \qquad x > 0$$

The point P(4, 6) lies on C.

The line l is the normal to C at the point P.

The region R, shown shaded in Figure 4, is bounded by the line l, the curve C, the line with equation x = 2 and the x-axis.

Show that the area of R is 46 (Solutions based entirely on graphical or numerical methods are not acceptable.)