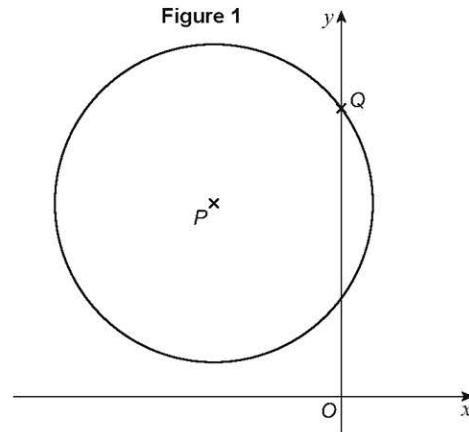


Figure 1 shows a circle.



The centre of the circle is  $P$  and the circle intersects the  $y$ -axis at  $Q$  as shown in Figure 1.

The equation of the circle is  $x^2 + y^2 = 12y - 8x - 27$

9 (a)

Express the equation of the circle in the form

$$(x - a)^2 + (y - b)^2 = k$$

where  $a$ ,  $b$  and  $k$  are constants to be found.

[3 marks]

9 (b)

State the coordinates of  $P$

[1 mark]

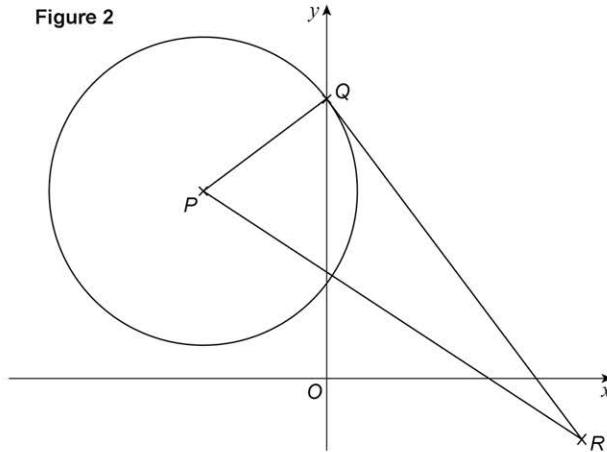
9 (c)

Find the  $y$ -coordinate of  $Q$

[2 marks]

9 (d)

The line segment  $QR$  is a tangent to the circle as shown in Figure 2 below.



The point  $R$  has coordinates  $(9, -3)$ .

Find the angle  $QPR$

Give your answer in radians to three significant figures.

[3 marks]